## TOPIC 20-3: ROTATIONS

Rotations: A transformation about a point $P$, known as the center of rotation, such that each point and its image are the same distance from $P$.

## Two types:



Determined by degrees:
$90^{\circ}$ :
270 ${ }^{\circ}$
$180^{\circ}$ :
$360^{\circ}$ :

Rotational Symmetry: A figure in the plane has rotational symmetry when the figure can be mapped onto itself by a rotation of $180^{\circ}$ or less about the center of the figure.
EXAMPLE 1: Describe each rotation \& tell if the figure has rotational symmetry.
a)

b)
$D \rightarrow Q$
c)


EXAMPLE 2: Draw the resulting triangles when the triangle is rotated $90^{\circ}, 180^{\circ}$, and $270^{\circ}$ clockwise about the origin.


After $90^{\circ}$ Rotation: After $270^{\circ}$ Rotation:
A' $\qquad$ ,
$\qquad$
$\qquad$ , _
B' $\qquad$ ,
$\qquad$
$\qquad$ , $\qquad$
C' $\qquad$ , $\qquad$ )
C' $\qquad$ , __

After $180^{\circ}$ Rotation:
$\mathrm{A}^{\prime}($ $\qquad$ ,
 B' $\qquad$ , $\qquad$
$\qquad$ , __

EXAMPLE 3: Rotate the figure below $90^{\circ}$ clockwise about the origin and define its new coordinates.

$\qquad$
$\qquad$
,


C' $\qquad$ ,

D' $\qquad$ ,

$\qquad$ ,


EXAMPLE 4: Rotate the figure below $180^{\circ}$ about the origin and define its new coordinates.

$\qquad$ ,
$E^{\prime}($ $\qquad$

$F^{\prime}$ $\qquad$ , $\qquad$

EXAMPLE 5: Using the figure in EXAMPLE 4, find the equation of the line containing $\overline{F D}$.

EXAMPLE 6: Rotate the figure below $90^{\circ}$ counter-clockwise about the origin and define its new coordinates.



EXAMPLE 7: A ferris wheel has a radius of 106 feet and takes 40 seconds to make a complete rotation. A car starts at position (106, 0). What are the approximate coordinates of the car's location after 5 seconds?

