## FUNCTION APPLICATIONS WITH GRAPHS

Draw sketches as necessary, show all work, and simplify answers.

1. A cylinder is generated by rotating a rectangle with perimeter 12 inches about one of its sides.

|  | a) If the radius of the cylinder is $x$, express the height, $y$, of <br> the cylinder in terms of $x$. |
| :--- | :--- |
|  | b) Express the volume of the cylinder, $V$, in terms of $x$, the <br> radius. |
|  | c) Find the volume of the cylinder when the radius is 4 <br> inches. |

2. A rectangle is bounded by the x-axis and the semicircle with radius 12 and center at $(0,0)$.
a) Sketch a picture of the problem.

|  | b) Write the equation of the semicircle. |
| :--- | :--- | :--- |
|  | c) Give the coordinates on the graph (vertices of rectangle) <br> in terms of $x$. |
|  | d) Write the area, A, of the rectangle as a function of $x$. |


|  | e) Find the area when $x=9$. Round to the nearest tenth. |
| :--- | :--- |

3. The portion of the vertical line through the point ( $x, 0$ ) that lies between the $x$-axis and the graph of $y=\sqrt{x}$ is revolved about the $x$-axis.

|  | a) Give the coordinates on the graph in terms of $x$. |
| :--- | :--- |
|  | b) Express the area, $A$, of the resulting disk (i.e. circle) as a <br> function of $x$. |
|  | c) Find the area of the disk if $x=9$. |

4. The area bounded by a vertical line through the point ( $x, 0$ ), the line $y=5$, and the $y$-axis is revolved around the $x$-axis.

|  | a) Give the coordinates of the point of intersection of the <br> vertical line passing through ( $x, 0$ ) and the line $y=5$ in <br> terms of $x$. |
| :--- | :--- |
|  | b) Find the volume of the resulting solid in terms of $x$. |
|  | c) Find the volume when $x=3$. |

