PER.

## NAME\_

## \_\_\_\_DATE\_\_\_\_\_

## FUNCTION APPLICATIONS WITH GRAPHS

## Draw sketches as necessary, show all work, and simplify answers.

1. A cylinder is generated by rotating a rectangle with perimeter 12 inches about one of its sides.

 a) If the radius of the cylinder is x, express the height, y, of the cylinder in terms of x.
 b) Express the volume of the cylinder, V, in terms of x, the radius.
 c) Find the volume of the cylinder when the radius is 4 inches.

2. A rectangle is bounded by the x-axis and the semicircle with radius 12 and center at (0, 0).

a) Sketch a picture of the problem.

 b) Write the equation of the semicircle.
 c) Give the coordinates on the graph (vertices of rectangle) in terms of x.
 d) Write the area, A, of the rectangle as a function of x.

	e) Find the area when $x = 9$ . Round to the nearest tenth.

3. The portion of the vertical line through the point (x, 0) that lies between the x-axis and the graph of  $y = \sqrt{x}$  is revolved about the x-axis.

 a) Give the coordinates on the graph in terms of x.
 b) Express the area, A, of the resulting disk (i.e. circle) as a function of x.
 c) Find the area of the disk if $x = 9$ .

4. The area bounded by a vertical line through the point (x, 0), the line y = 5, and the y-axis is revolved around the x-axis.

 a) Give the coordinates of the point of intersection of the vertical line passing through (x, 0) and the line $y = 5$ in terms of x.
 b) Find the volume of the resulting solid in terms of x.
 c) Find the volume when x = 3.